

Measures of Dispersion (Deviation)

**Mean Deviation, Standard
Deviation and Error
Variance**

**Statistical
Investigation**

**5. Analysis
of data**

A. Average

B. Dispersion

D. Correlation

Similarities? Differences?

	S1	S2	S3	S4	S5	Total	Mean
A	16	16	16	16	16	80	16
B	14	15	16	17	18	80	16
C	3	8	17	24	28	80	16

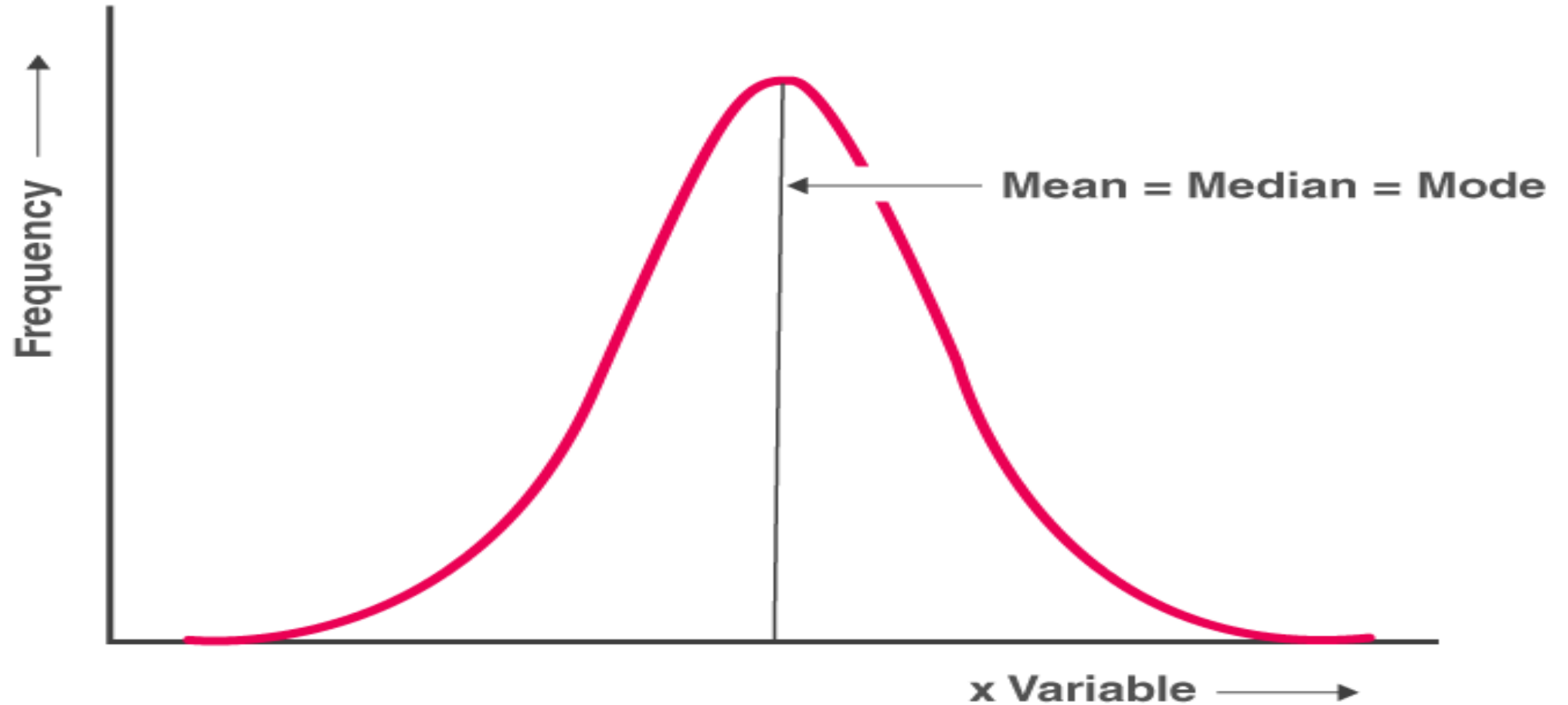
Normal Distribution

- The area under a normal curve has a *normal distribution* (Gaussian distribution)
- Properties of a normal distribution
 - It is symmetric about its mean
 - The highest point is at its mean
 - The height of the curve decreases as one moves away from the mean in either direction, approaching, but never reaching zero

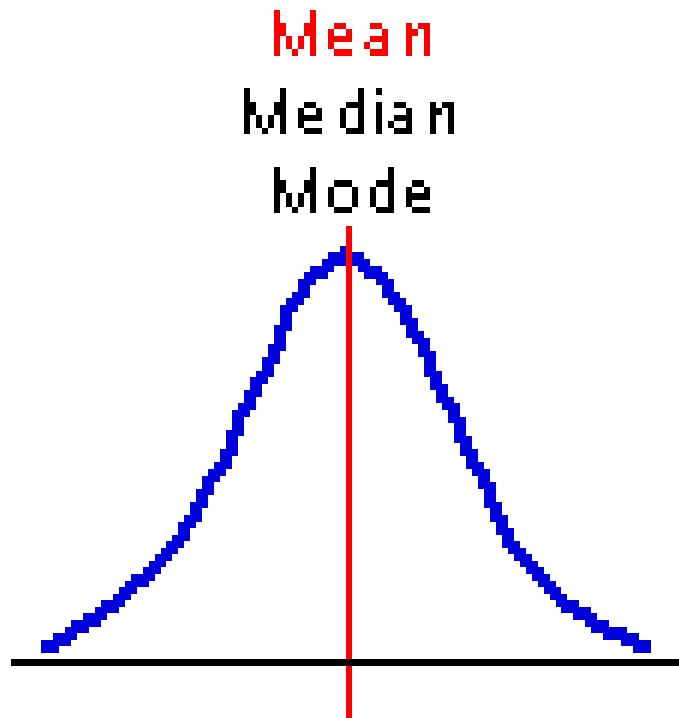
Skewed Distribution

- **The data are not distributed symmetrically in skewed distributions**
 - Consequently, the mean, median, and mode are not equal and are in different positions
 - Scores are clustered at one end of the distribution
 - A small number of extreme values are located in the limits of the opposite end
- **Skew is always toward the direction of the longer tail**
 - Positive if skewed to the right
 - Negative if to the left

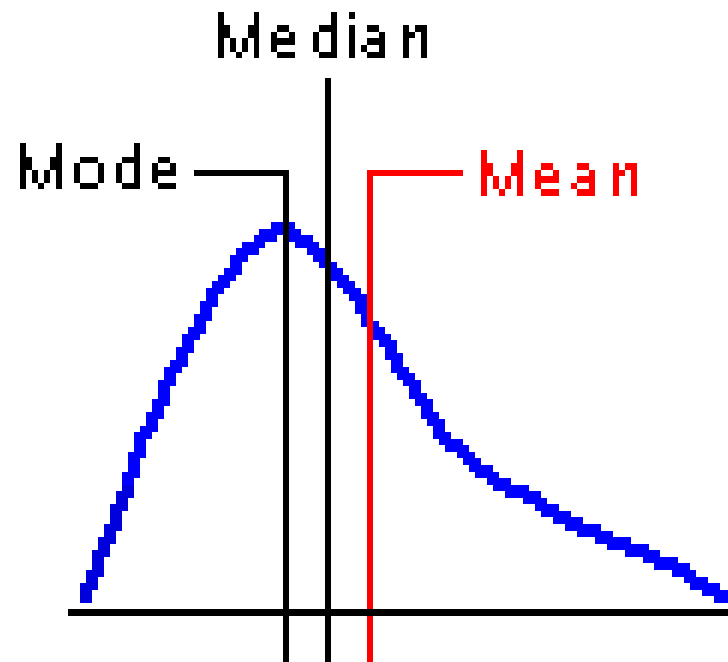
Normal Distribution



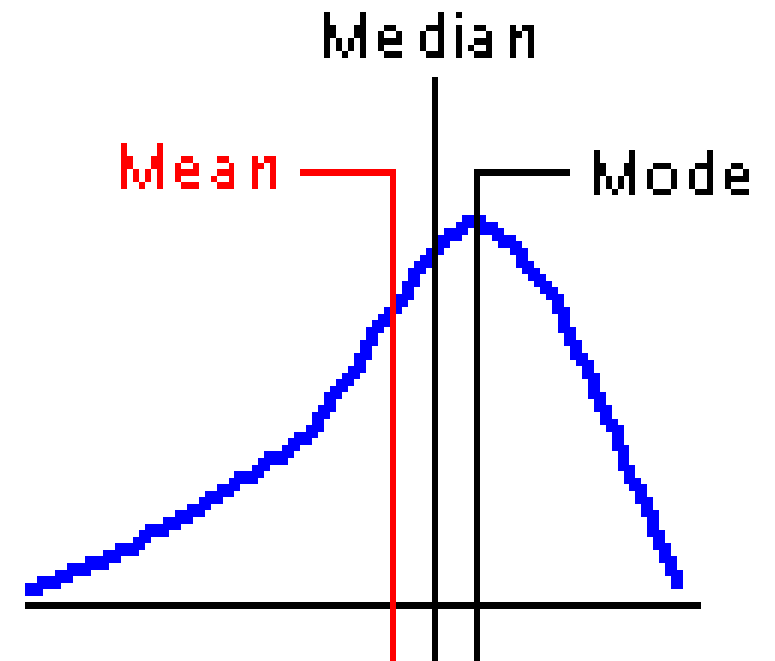
Skewed Distribution



Symmetrical
Distribution



Positive
Skew



Negative
Skew

Measures of Dispersion

- It is the degree of the scatter
- It is the measure of the variations of the items
- It is the degree to which numerical data tend to spread about an average value

Measures of Dispersion

Objectives –

1. To determine the reliability of an average
2. To serve as a basis for the control of variability
3. To compare two or more series with regard to their variability
4. To facilitate the use of other statistical measures

Measures of Dispersion

```
graph TD; A[Measures of Dispersion] --> B[Mean Deviation]; A --> C[Standard Deviation]
```

**Mean
Deviation**

**Standard
Deviation**

Merits and Demerits of Mean Deviation

Merits

- Readily understood
- Based on all observations
- Less affected by extreme items
- Better measure for comparison
- Flexible because can also be calculated by Median

Demerits

- Not used for further mathematical treatments
- Can not be calculated in open end classes
- May not give accurate results

Mean Deviation/ Average Deviation

- It is based on all the items of a distribution
- It is an average amount of scatter of items in a distribution

$$\frac{\Sigma(x - \bar{x})}{n} \quad \text{or} \quad \frac{\Sigma(dx)}{n}$$

Standard Deviation

- It is introduced by Karl Pearson in 1893
 - It is positive square root of the arithmetic mean of the squares of the deviation of the given observations
 - Represented by Greek letter sigma ' σ '
1. Direct method – Deviation taken from actual mean
 2. Short cut method – Deviation taken from assumed mean

Direct method

1. Find out the actual mean (\bar{x})
2. Find out deviation from mean ($x - \bar{x}$)
3. Square the deviation of each value and take the total of squared deviations ($\Sigma(x - \bar{x})^2$)
4. Divide the total by the number of observations $\frac{\Sigma(x - \bar{x})^2}{N}$
5. Find the square root of the product

$$SD = \sqrt{\Sigma \left(\frac{x - \bar{x}}{N} \right)^2}$$

Short cut method

1. Take the assumed mean (A)
2. Find deviation from assumed mean ($x-A=d$)
3. Square the deviation of each value (d^2) and take the total of squared deviations ($\sum d^2$)
4. Apply the formula

$$\sqrt{\frac{\sum d^2}{N} - \left[\frac{\sum d}{N}\right]^2}$$

Standard Deviation

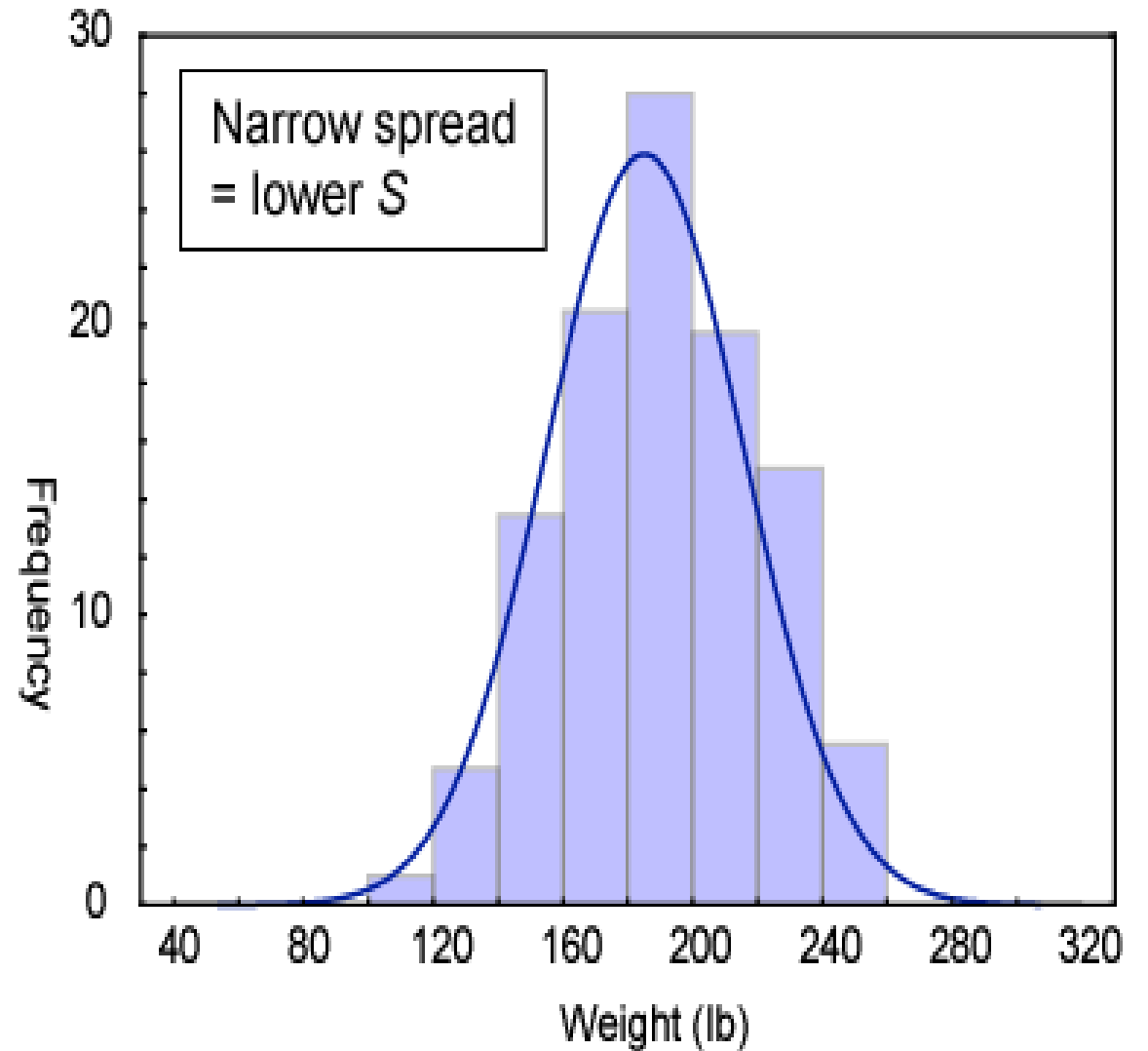
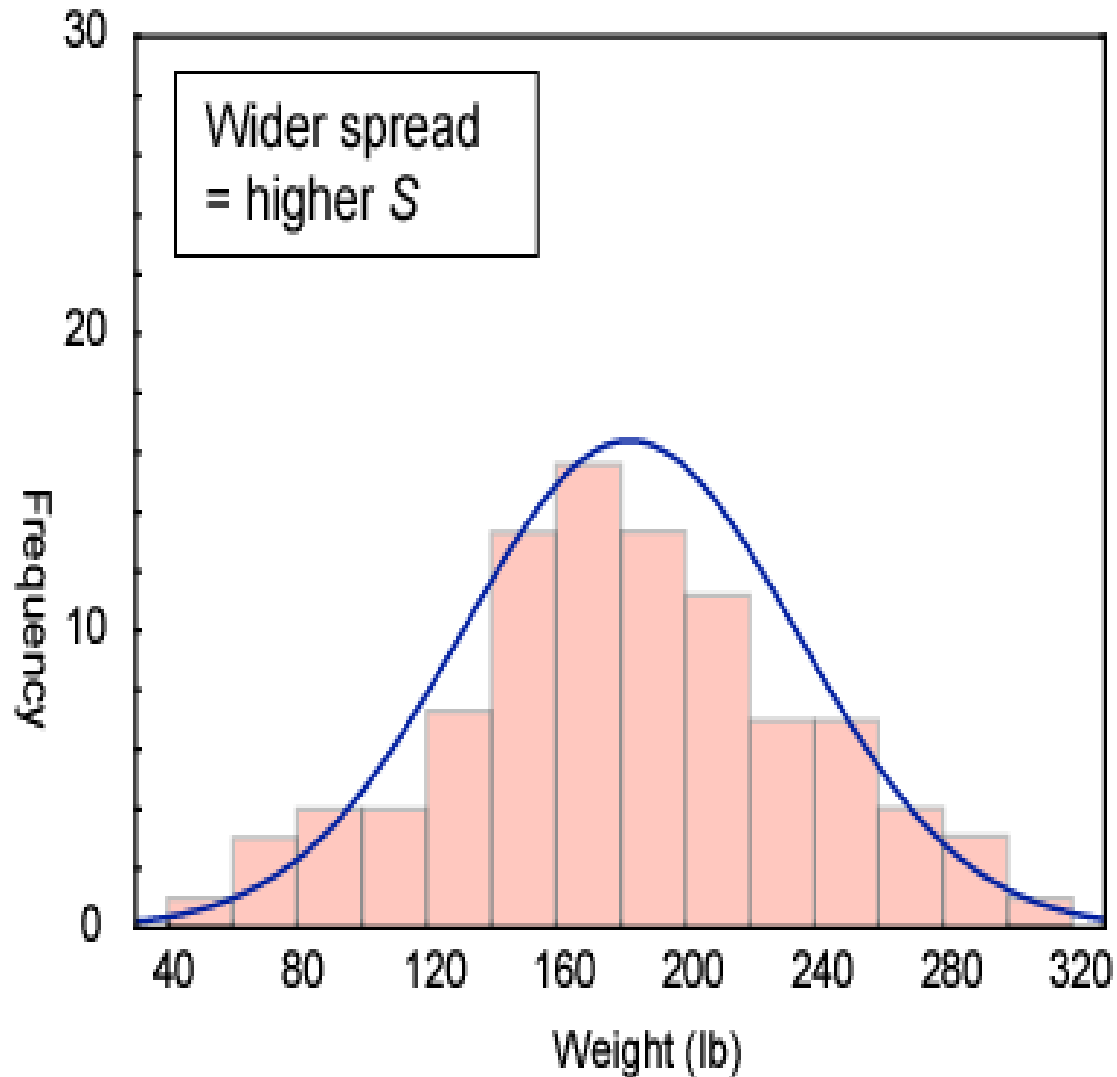
Merits

- Rigidly defined and based on all observations
- Most important for authenticity of data and widely used
- Possible for further algebraic treatments
- Squaring the deviations make all of them positive

Demerits

- Not easy to understand
- Affected by the values of every items in the series

Wide spread results in higher SDs
narrow spread in lower SDs



Standard Error

It is a statistical constant which measures the dispersion of the sample means around the total population mean

$$\frac{SD}{\sqrt{N}}$$

Variance

It is the square of the standard deviation

$$\text{Variance} = \text{SD}^2$$

$$\text{SD}^2 = \text{Variance}$$

$$\text{SD} = \sqrt{\text{Variance}}$$

Coefficient of Variation

It was first developed by Karl Pearson

- The standard deviation is an absolute measure of dispersion. It is expressed in terms of units in which the original figures are collected and stated
- But the deviation from two different units can not be compared (weight in g and length in cm)
- Therefore, the standard deviation must be converted into a relative measure of dispersion for the purpose of comparison
- This is known as Coefficient of variation (CV)

- If the coefficient of variation is greater, then it is said to the group is more variable, less stable, less uniform or less homogenous

$$\text{Coefficient of variation} = \frac{\text{Standard Deviation}}{\text{Mean}} \times 100$$

- It is most useful in comparing the variability of several different samples each with different mean

Ex . Air pollution study at different sites and at different time intervals